Modeling island effects with probabilistic tier-based strictly local grammars over trees

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Gradience and Syntactic Formalisms

How does one account for gradience in grammatical acceptability judgments?

Two possibilities:

- 1 It's not in syntax, so don't worry
- 2 Extend formalisms to allow for non-discrete judgments

This work

We investigate using the second strategy with new formalisms from subregular linguistics.

Collaborators

This is joint work across two institutions: UCI and Stony Brook





Charlie Torres Kenneth Hanson





Thomas Graf Connor Mayer

Outline

1 TSL and pTSL

2 Modeling syntactic dependencies using (p)TSL over trees

3 Modeling study

4 Modeling study results

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$$\odot$$

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$$T := \{ \acute{\sigma} \} \qquad \qquad G = \{ \acute{\sigma} \acute{\sigma}, \rtimes \ltimes \}$$

TSL grammars prohibit certain substrings on a tier projection.

► Non-local dependencies become local on the tier.

$$T := \{ \acute{\sigma} \} \qquad \qquad G = \{ \acute{\sigma} \acute{\sigma}, \rtimes \ltimes \}$$

Input: $\rtimes \ \ \sigma^* \ \ \sigma \ \ltimes$

TSL grammars prohibit certain substrings on a tier projection.

$$T := \{ \acute{\sigma} \} \qquad \qquad G = \{ \acute{\sigma} \acute{\sigma}, \rtimes \ltimes \}$$

Tier:

$$\dot{\sigma}$$
 $\dot{\sigma}$
 κ

 |
 |
 |

 Input:
 $\dot{\sigma}$
 σ^*
 $\dot{\sigma}$

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$$\begin{array}{c|cccc} \mathbf{Tier:} & \rtimes & \acute{\sigma} & \acute{\sigma} & \ltimes \\ & & & & & \\ & & & & & \\ \mathbf{Input:} & \rtimes & \acute{\sigma} & \sigma^* & \acute{\sigma} & \ltimes \end{array}$$

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Acceptability ratings

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Acceptability ratings

(Albright and Hayes 2003; Daland et al. 2011)

Production frequencies

(Hayes and Londe 2006; Zuraw and Hayes 2017)

Example: Uyghur backness harmony (simplified)

Description: Vowels in a word must agree in backness

► The vowel /i/ is transparent (relevant later).

TSL grammar $G = \{aaa, aaa, uy, \dots\}$ $T = \{aa, a, o, o, y, u\}$ Data $p\underline{æ}n-l\underline{æ}r$ 'science-PL' * $p\underline{æ}n-l\underline{a}r$

<u>a</u>t-l<u>a</u>r 'horse-PL' *<u>a</u>t-l<u>æ</u>r Gradient blockers

Uvulars are gradient blockers in Uyghur wug tests (Mayer 2021)

Production rates with no uvular:

pæt-lær (100%) vs. pæt-lar (0%)

Production rates with uvular:

pæq-lær (75%) vs. pæq-lar (25%)

Increases tendency for back suffixes, but not categorically!

String: \rtimes p æ q l a r \ltimes



$$T = \{\texttt{æ, a, \phi, o, y, u}\}$$



$$T = \{\texttt{æ, a, \phi, o, y, u}\}$$



$$T = \{ \mathbf{a}, \mathbf{a}, \mathbf{\phi}, \mathbf{o}, \mathbf{y}, \mathbf{u}, \mathbf{q} \}$$
Does /q/ project?



 $T = \{ \texttt{æ, a, \phi, o, y, u, \underline{q}} \}$

Does /q/ project?



In either case, predicts categorical blocking or failure to block.

pTSL generalizes TSL by making projection *probabilistic*.

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Score: Sum of the probabilities of all grammatical projections.

A simple case

String: × p æ q l a r ×

Modelling

A simple case



TSL and pTSL	(p)TSL №	lovement	M	odelling	Results	Conclusio
A simple case						
		1×1 >	<.75× 1	\times 1 \times 1	= 0.75	
Projection 1	l: ⋊	æ		a 	×	
String	g: ⋊	pæ	q l	a r	\ltimes	

TSL and pTSL	(p)TSL N	/lovement		Mod	lelling		Results	Conclus
A simple case								
		1×1	$\times.75$	$\times 1$	$\times 1 \times$	1	= 0.75	
Projection 1	l: ⋊	æ	:		a	×		
String	7 : ×	 рæ	a	Т	a 	r 🗵		
	5							
Projection 2	2 : ⋊	æ	, q		à	\ltimes		

TSL and pTSL	(p)TSL N	lovement	Modelling	F	Results	Conclusion
A simple case						
		$1 \times 1 \times .7$	$5 \times 1 \times 1 \times$	1	= 0.75	
Projection 1	l: ⋊	æ	a	\ltimes		
String	. . M	 n 20 (a 1 a 	r 🗵		
Stille	5. 7					
Projection 2	2: ⋊	æd	a a	\ltimes		
		$1 \times 1 \times .2$	$5 \times 1 \times 1 \times$	1	= 0.25	

A simple case



Modelling

A simple case



Score for /pæqlar/: 0.25

× pæqiqlar ×





Modelling



















How does this apply to syntax?

TSL and pTSL	(p)TSL Movement		Conclusion

How does this apply to syntax?

1 First, we will look at how TSL grammars over trees can regulate syntactic movement.

TSL and pTSL	(p)TSL Movement		Conclusion

How does this apply to syntax?

- First, we will look at how TSL grammars over trees can regulate syntactic movement.
- 2 Second, we will see if this can be extended in the same way to handle gradient syntactic judgments.

Who does Mary think might buy what?

Who does Mary think $\langle who \rangle$ might $\langle who \rangle$ buy what?

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nom⁻, wh⁻

Who does Mary think $\langle who \rangle$ might $\langle who \rangle$ buy what?

nom⁺ nom⁻, wh⁻

Who does Mary think $\langle who \rangle$ might $\langle who \rangle$ buy what?

 wh^-

Who does Mary think $\langle who \rangle$ might $\langle who \rangle$ buy what? wh⁺ wh⁻

Who does Mary think $\langle who \rangle$ might $\langle who \rangle$ buy what?

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TSL and pTSL	(p)TSL Movement	Modelling	Results	Conclusion
Movement in	MGs is tier-based	strictly l	ocal (TSL)	
		does $_{\rm wh^+ C^-}$		
	V^+	ε nom ⁺ T ⁻		
		think		
	T Mary	r+ D+ V- might		
	D^{-} {nom ⁻	$V^+ \text{ nom}^+ T^-$		
		$buy_{D^+ \ D^+ \ V^-}$		
	D^{-}		vhat \mathbb{D}^-	







Feature checking as a constraint on each f-tier

Every f⁺ has exactly 1 f⁻ among its daughters.
 Every f⁻ has f⁺ as its mother.

(1) * What did John complain about the fact that Mary brought (what) to the party?

```
did :: T^+wh^+C^-
                   \varepsilon :: V^+ nom^+ T^-
               \operatorname{complain} :: P^+D^+V^-
  John :: D^{-} {nom<sup>-</sup>} about :: D^{+}P^{-}
                                   the :: N^+D^-
                                  fact :: C^+N^-
                                  that :: T^+C^-
                                 \varepsilon :: V^+ nom^+ T^-
                            brought :: P^+D^+D^+V^-
Mary :: D^{-} {nom<sup>-</sup>} what :: D^{-} {wh<sup>-</sup>} to the party :: P^{-}
```

(1) * What did John complain about the fact that Mary brought (what) to the party?

did :: $T^+wh^+C^ \varepsilon :: V^+ nom^+ T^$ did :: $T^+wh^+C^ \operatorname{complain} :: P^+D^+V^$ what :: $D^{-} \{wh^{-}\}$ John :: D^{-} {nom⁻} about :: $D^{+}P^{-}$ the :: $N^+D^$ fact :: $C^+N^$ that :: $T^+C^ \varepsilon :: V^+ nom^+ T^$ brought :: $P^+D^+D^+V^-$ Mary :: D^{-} {nom⁻} what :: D^{-} {wh⁻} to the party :: P^{-}

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                               that :: T^+C^-
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did :: T^+wh^+C^-
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                                                         did :: T^+wh^+C^-
                                                                                      did :: T^+wh^+C^-
                                                                       ╰╉╴╴╖
             complain :: P^+D^+V^-
                                                        what :: D^{-} \{wh^{-}\}
                                                                                     fact :: C^+N^-
  John :: D^{-} {nom<sup>-</sup>} about :: D^{+}P^{-}
                                                                                    what :: D^{-} {wh^{-}}
                               the :: N^+D^-
                               fact :: C^+N^-
                               that :: T^+C^-
                              \varepsilon :: V^+ nom^+ T^-
                         \mathrm{brought}::\ P^+D^+D^+V^-
Mary :: D^{-} {nom<sup>-</sup>} what :: D^{-} {wh<sup>-</sup>} to the party :: P^{-}
```

 P^{-}

▶
$$P_{proj}(\text{fact}) = 0.7$$

▶ $P_{proj} = 1$ for all wh nodes, 0 otherwise

$$\begin{array}{c} \operatorname{did}:: \mathbf{T}^+ \mathbf{w} \mathbf{h}^+ \mathbf{C}^- \\ \varepsilon :: \mathbf{V}^+ \mathbf{nom}^+ \mathbf{T}^- \\ \hline \\ \operatorname{complain}:: \mathbf{P}^+ \mathbf{D}^+ \mathbf{V}^- \\ \end{array}$$

$$\begin{array}{c} \operatorname{John}:: \mathbf{D}^- \left\{ \operatorname{nom}^- \right\} & \operatorname{about}:: \mathbf{D}^+ \mathbf{P}^- \\ & \operatorname{the}:: \mathbf{N}^+ \mathbf{D}^- \\ & \operatorname{fact}:: \mathbf{C}^+ \mathbf{N}^- \\ & \operatorname{that}:: \mathbf{T}^+ \mathbf{C}^- \\ & \varepsilon :: \mathbf{V}^+ \operatorname{nom}^+ \mathbf{T}^- \\ & \operatorname{brought}:: \mathbf{P}^+ \mathbf{D}^+ \mathbf{V}^- \\ \end{array}$$

$$\begin{array}{c} \operatorname{Mary}:: \end{tabular} \quad \mbox{the party}:: \end{tabular}$$





















Modeling Island Effects using pTSL over Trees

Remainder of this talk: a modeling study that captures gradient island effects in experimental acceptability judgments.

Fit P_{proj} to English experimental data from Sprouse et al. (2016).



Figure: Jon Sprouse

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Example:

- (2) a. Who t thinks [that John bought a car]? (non-island, matrix clause)
 - b. What do you think [that John bought t]? (non-island, embedded clause)
 - c. Who t wonders [whether John bought a car]? (island, matrix clause)
 - d. What do you wonder [whether John bought t]? (island, embedded)

Only sentences with extraction from an embedded clause over an island structure should be ungrammatical.

 Superadditivity: effect of these two factors together is greater than their individual effects.



Island types

We restricted ourselves to three subsets of island effects:

- Whether islands: *What do you wonder whether John bought t?
- **2** Complex NP islands: *Who did Mary deny the rumor that John likes *t*?
- **3** Adjunct islands: *Who did Mary complain because John likes *t*?

The Complex NP Constraint and Adjunct Island Constraint also apply to extraction out of relative clauses.

We treat both as involving wh features for simplicity.

Adapting the data

Each of these sentences has a Likert score assigned by the participants.

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We converted each sentence in the data set into dependency tree format.

Fitting the model

Some projection probabilities set a priori:

- Most nodes set to 0
- wh nodes set to 1

Free parameters: Blockers in the discrete analysis.

- ▶ that :: T⁺C⁻ (whether/adjunct islands)
- ▶ whether :: T⁺C⁻ (whether/adjunct islands)
- ▶ if :: T⁺C⁻ (whether/adjunct islands)
- all nodes whose feature annotation contains the substring C⁺N⁻ (complex NP islands)

Fitting the model

Free parameters fit to data set consisting of dependency trees with mean normalized Likert ratings.

Model assigns values in [0,1] to each tree.

We find projection probabilities that minimize the mean squared error between model and human scores.

Super-additivity: Humans vs. pTSL



Figure: Super-additivity in a pTSL model

Fit Projection Probabilities

Node	Projection probability
that :: T^+C^-	.46
C^+ N^-	.63
whether :: T^+C^-	.73
if :: T^+C^-	.89

Table: Fit projection probabilities

Higher probability means greater propensity to block and induce island effects.

Discussion

The model succeeds in some respects:

- Captures supperadditivity
- Relative badness of different types of islands.

The model fails in other respects:

- Overpredicts superadditivity in some cases
- Doesn't account for variability in non-island cases.

Discussion

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Some of the probabilities likely encode non-syntactic features:

- 'that' isn't typically considered a blocker.
- Encodes (non-syntactic?) decrease in acceptability between matrix and embedded extraction.

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Takeaways

- Converting a categorical TSL model to a probabilistic one is easy and empirically viable.
- The same computational structure can be applied to constraints in phonology and in syntax.
- pTSL over trees can capture superadditivity and gradience in syntactic island effects.

Take-home message

pTSL over trees lets us model gradience arising from grammatical factors.

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whether island



Adjunct island

