



## Overview

**Grammar** Most long-distance linguistic patterns are **tier-based strictly 2-local (TSL-2)** (McMullin 2016; Graf 2022; Hanson 2024).

**Learning** Pure TSL string languages are **efficiently learnable**, but multiple tiers present various difficulties. Heuser et al. (2024) propose an algorithm which learns syntactic blockers as **local constraints on paths**.

**This Work** Adapt the insights of Heuser et al. (2024) to produce an efficient TSL-2 learner which **factors out local constraints**.

**Bonus** We can derive a version of the **Height-Locality Connection** (cf. Keine 2019) which is not an inherent prediction of TSL-2.

## Tiers Over a-Strings

### TSL in a nutshell

1. Ignore the irrelevant items; the remainder form a **tier**.
2. Items on the tier are subject to **local constraints**.
3. **TSL-2**: constraint window contains only two items.

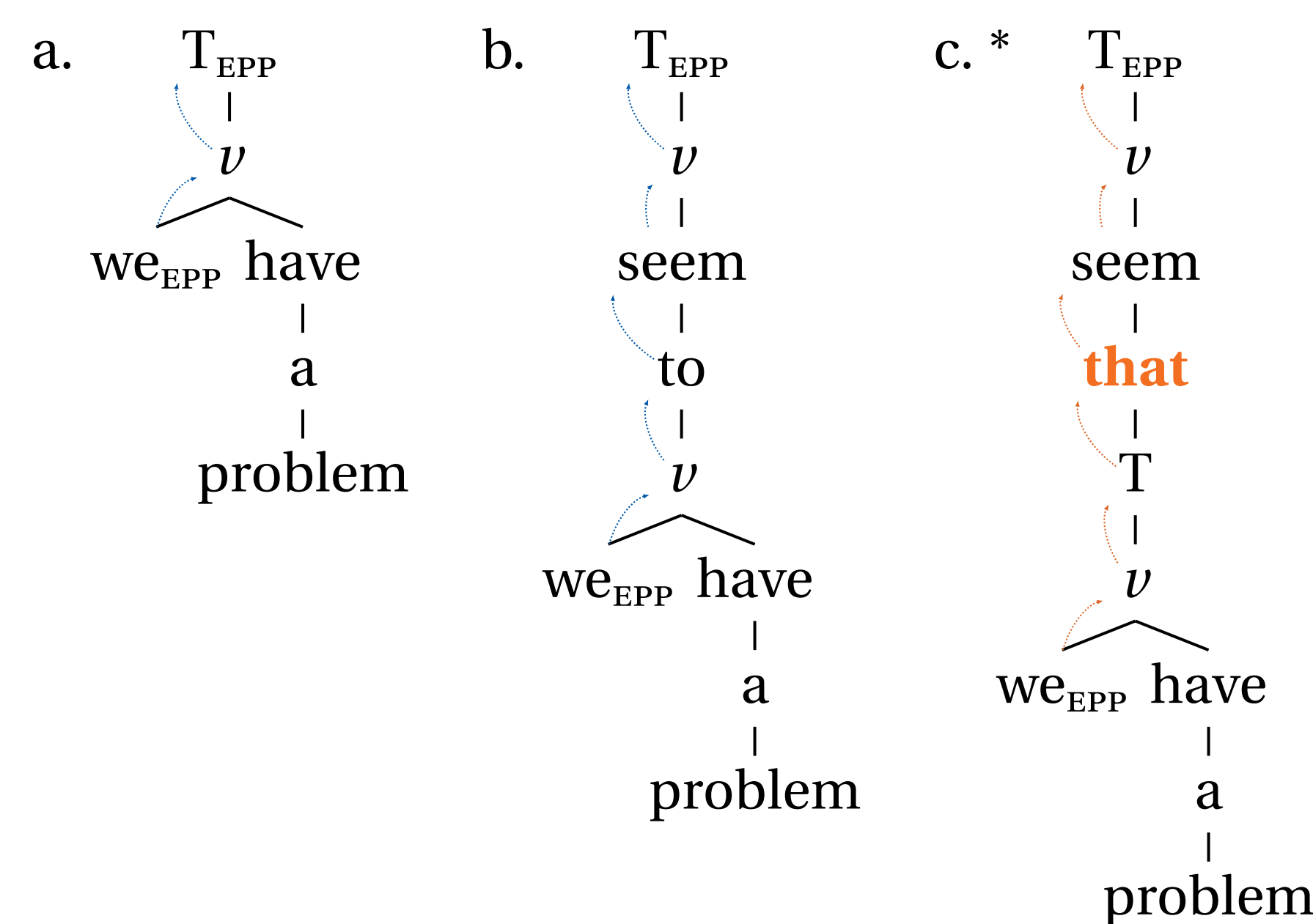
**Modeling movement** We use **a[ncestor]-strings** over MG dependency trees (Shafiei and Graf 2020). For each movement type:

- The tier contains only (i) movers, (ii) landing sites, and (iii) blockers.
- On the tier, a mover must be immediately followed by its landing site.

### Example: EPP-movement

- (1) EPP movement: C is a blocker, T is not
  - a. We [<sub>VP</sub> \_\_\_ have a problem].  
A-string:  $\times \cdot D_{EPP} \cdot v \cdot T_{EPP} \cdot \times$   
Tier:  $\times \cdot D_{EPP} \cdot T_{EPP} \cdot \times$
  - b. We seem [<sub>TP</sub> to \_\_\_ have a problem].  
A-string:  $\times \cdot D_{EPP} \cdot v \cdot T \cdot V \cdot v \cdot T_{EPP} \cdot \times$   
Tier:  $\times \cdot D_{EPP} \cdot T_{EPP} \cdot \times$
  - c. \*We seem [<sub>CP</sub> **that** \_\_\_ have a problem].  
A-string:  $\times \cdot D_{EPP} \cdot v \cdot T \cdot C \cdot V \cdot v \cdot T_{EPP} \cdot \times$   
Tier:  $\times \cdot D_{EPP} \cdot C \cdot T_{EPP} \cdot \times$

(2) Dependency trees for the above



(3) Target TSL-2 grammar for EPP-movement

$$T = \{D_{EPP}, T_{EPP}, C\}$$

$$G^- = \{D_{EPP} \cdot D_{EPP}, D_{EPP} \cdot C, D_{EPP} \cdot \times\}$$

### Important points

- A TSL grammar applies to **the entire structure** (here, every a-string).
- Each dependency gets its own grammar. The intersection of several TSL grammars is an **MTSL** grammar.
- This works for **agreement**, too (cf. Hanson 2024).

## Distributional Learning of Syntactic Blockers

### Heuser et al (2024) algorithm

- **Memorizes** bigrams along attested movement paths → approximately an SL learner (Heinz 2010).
- **Generalizes** from individual items to categories when permitted by the Tolerance Principle (Yang 2016).
- **Missing bigrams** correspond to blockers.

**Example** Given data like (1a) and (1b), learns that EPP movement is possible out of VP/*v*P/TP but not CP.

(4) Sample output for EPP-movement

$$G^+ = \{D_{EPP} \cdot V, D_{EPP} \cdot v, V \cdot v, v \cdot T_{EPP}, v \cdot T, T \cdot V\}$$

- Advantages** • Efficient, online learner. • Makes correct generalizations based on a realistic input distribution. • Works for a variety of syntactic blockers.

### Disadvantages

Resulting grammar looks like an SL grammar, but requires a-strings to be truncated to movement paths.

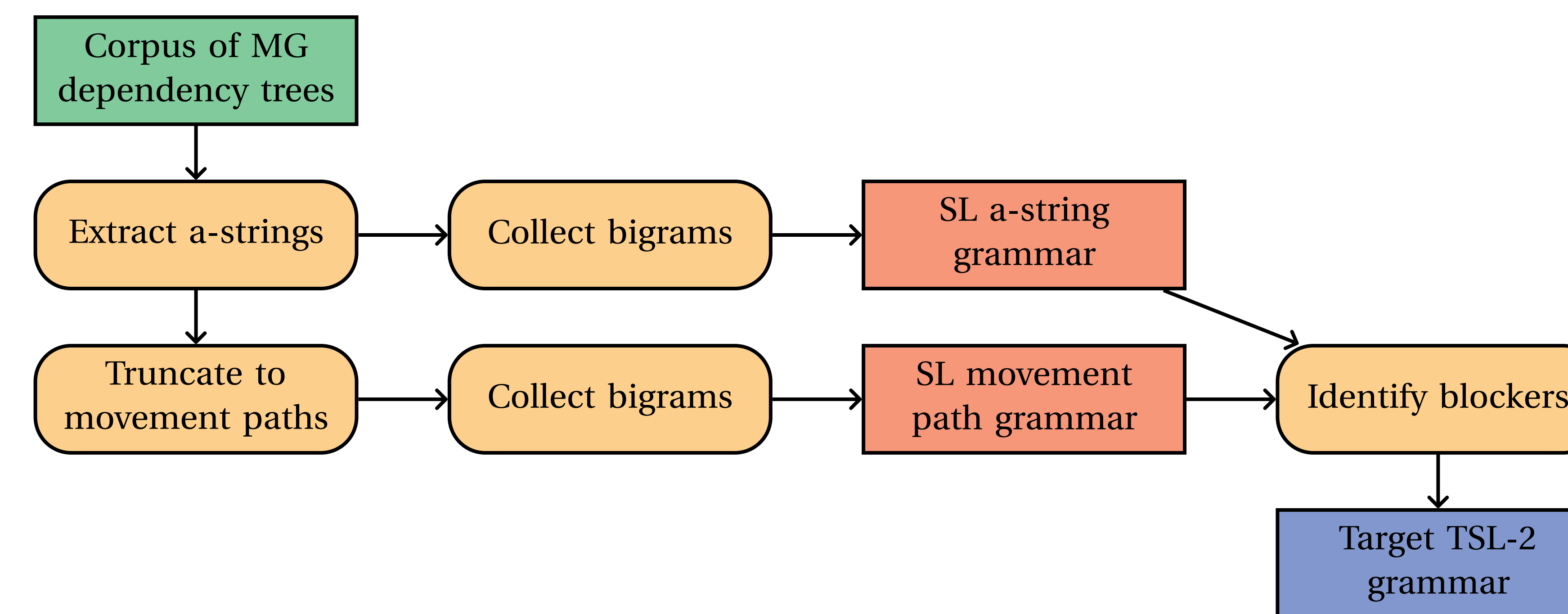
→ Implicitly increases computational complexity to IBSP (Graf 2017).

→ Neither SL nor IBSP matches the typology of long-distance dependencies as well as TSL-2.

## Learning Tiers from Paths

### Proposal

- **Truncate** a-strings to movement paths **only during learning**.
- **Construct** movement path grammar  $G_M$  as above, **plus** a grammar  $G_L$  constructed for arbitrary a-strings, which reflects local constraints.
- **Compare**  $G_M$  and  $G_L$  to identify blockers, then construct the desired TSL-2 grammar.



## Implications for Locality

**Height-Locality Connection** “Higher” categories in a functional hierarchy are subject to fewer locality restrictions (Keine 2019). This follows from our learner:

- DPs can start in Comp-VP, so every category from V to the landing site must be transparent.
- Will allow extraction from higher categories only if there is positive evidence.

Dependency	English			Hindi		
	Location	CP	TP	CP	TP	vP
$\phi$ -agreement	T	*	✓	*	*	✓
A-movement	T	*	✓	*	*	✓
Wh-movement	C	✓	✓	*	✓	✓
Rel-movement	C	✓	✓	✓	✓	✓

## Insights from Learnability Theory

### Learning TSL string languages

- TSL allows free insertion/deletion of non-tier elements → heuristic for tier detection (Jardine and McMullin 2017).
- Pure TSL-*k* (string) grammars can be learned in the limit from positive data, online, by collecting all (*k*+1)-grams (Lambert 2021).
- An older TSL-2 learner tracks the set of possible interveners for each pair of symbols (Jardine and Heinz 2016).

### Important points

- The Heuser et al. (2024) algorithm tracks similar information as existing TSL learners, but interprets it differently.
- None of the above learners deal with interacting constraints on different tiers → need to compare against *expected* *k*-grams, e.g. an SL grammar for selection and functional hierarchies.

## Related Work

- Pearl and Sprouse (2013) track trigram probabilities in order to learn syntactic islands.
- Belth (2023) presents a Tolerance Principle-based algorithm for learning vowel harmony, encoded as a TSL-2 grammar.
- McMullin et al. (2019) develop an algorithm which learns a subclass of the MTSL-2 string languages. Swanson (2024) does the same for MTSL-2 tree languages.

## Future Work

**Empirical coverage** Can the proposed model be used to learn dependent case, and other dependencies between >2 elements?

**Typology** Contra Keine (2019), the proposed model predicts that exceptions to the height-locality connection are possible under the right conditions – do these exist?

**Learnability** A proof is needed to show that SL constraints can be successfully factored out in all cases. Also, can we handle interactions between many tiers under realistic conditions?

## References and Acknowledgments

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