# A Tier-Based Model of Syntactic Agreement

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# 1 Introduction

### ■ Some (paradoxical) properties of agreement ■

Usually	but
Applies over a distance	Subject to blockers
Blockers are predictable	Vary across dependencies/languages
Targets the closest visible DP	Which DPs are visible varies
Probe c-commands goal	Sometimes reversed
One probe $\leftrightarrow$ one goal	Sometimes many-to-one

#### ■ Overview ■

**Main claim:** Agreement patterns are **tier-based strictly local (TSL)**, mirroring findings on movement (Graf 2022b) and case (Hanson 2023b).<sup>1</sup>

#### Why this matters:

- · Limits structural configurations
- Defines parameters for variation
- · Provides a unified model of locality restrictions
- · Shows parallels within/across domains
- · Derives typology from issues of efficient computation

#### Roadmap

- 1. What is a TSL pattern?
- 2. A TSL model of agreement
- 3. Consequences for locality
- 4. Typological variation
- 5. Parallels with phonology
- 6. Strengths and limitations of the model

# 2 TSL patterns

# ■ What is a TSL pattern? ■

- 1. Ignore the irrelevant items and treat the rest as if adjacent
- 2. All constraints must be stated within a fixed-size moving window

#### **Example: Vowel harmony**

i/u/o obey front-back harmony, *e* is transparent/neutral, *a* is opaque

All elements: k, b, l, i, e, u, o, a	k <b>u</b> bulo	uuo	1
Tier elements: i, u, o, <b>a</b>	kibilo	i <mark>io</mark>	X
Invisible elements: k b l e	kubelo	uo	1
	kibelo	io	X
Constraints: *10, *10, *01, *01	kubalo	uao	1
	kibalo	iao	1

Word

Tier

#### ■ More about TSL ■

- Originally defined to model phonological patterns (Heinz et al. 2011)
- Argued to be relevant in syntax as well (Graf 2022a)
- Inspired by but distinct from autosegmental phonology (Goldsmith 1976)
- Special relational structure (tier successor) with very weak constraint logic (banned substrings) (Lambert et al. 2021)
- By hypothesis, we only need a window of size two (McMullin 2016)



TSL string model with constraint window of size two

See Appendix A.1 for another example and a formal definition.

# 3 A TSL Model of Agreement

#### ■ Setup ■

#### Assumptions:

- Bare phrase structure, feature-driven selection, movement, ...
- Agreement between elements with initially unvalued features (probes) and elements which provide those values (goals)<sup>2</sup>

Question: What are the possible arrangements of probes and goals for agreement?

Answer: They are TSL constraints on the search path of the probe.

<sup>&</sup>lt;sup>1</sup>This is an informal presentation of an analysis done in the framework of MG derivation trees, recast in terms of mainstream Minimalism. See Hanson (2023a) for a more formal presentation (available at https://www.kennethhanson.net/files/hanson-nyubb2023-agreement-slides.pdf).

<sup>&</sup>lt;sup>2</sup>I use the term **agreement** rather than **Agree** to indicate that we are not presupposing a particular version of the Agree operation, nor dealing with other phenomena that are sometimes subsumed under Agree.

# ■ The search path ■

The search path follows the derivational command (d-command) relation (Graf and Shafiei 2019).

- Head < Spec < Comp
- d-command order  $\approx$  height of XP
  - $\approx$  order of last merge
  - $\approx$  reverse order of selection
- Projections of a head are not distinguished.
- · At each branching point, follow the complement spine (Graf and De Santo 2019).

See Appendix A.2 for how this works using derivation trees.

### ■ The TSL analysis ■

General principle: a probe must be immediately followed by its goal on a tier projected from the search path (and vice versa).

**Notation:**  $p\phi = \text{probe}$   $g\phi = \text{actual goal}$   $\phi = \text{other potential goal}$ 

### Example: (canonical) subject-verb agreement

Tier elements: All agreeing elements (T/D) and blockers (C)  $T_{[p\phi]} \cdot D_{[\phi]}, T_{[p\phi]} \cdot C, T_{[p\phi]}, T_{[p\phi]} \cdot D_{[p\phi]}, T_{[p\phi]} \cdot D_{[p\phi]}, \dots$ Constraints:

# ■ The TSL analysis – example ■

Path:

Tier:

Violations: n/a



For simplicity, we substitute most items with their category labels.

ex. 'The cat chases the rats.'



# 4 Consequences for locality

# Consequences for locality

- Minimality: if another potential goal intervenes on the tier, agreement is blocked.
- Invisibility: if a DP is omitted from the tier, long-distance agreement is possible. - e.g. agreement across *there*, case-sensitive agreement
- Blocking: if a non-agreeing element intervenes on the tier, agreement is blocked. - e.g. probe horizons (Keine 2019), defective intervention

### Minimality

If another potential goal intervenes on the tier, agreement is blocked.



# Invisibility

If a DP is omitted from the tier, long-distance agreement is possible.



in the garden

#### We can handle optional default agreement in several ways. Ask me if you are interested.

#### Blocking

If a non-agreeing element is projected on the tier, agreement is blocked.



out there too

Assume for the sake of demonstration that expletive "it" is inserted late and does not agree.

#### ■ Locality – summary ■

Locality phenomena derive from TSL with a window of size two, a.k.a. TSL-2.

• Minimality: closer potential goal intervenes

$$T_{[p\phi]} \dots D_{[\phi]} \dots D_{[g\phi]}$$

• Invisibility: hypothetical goal does not appear on tier

$$T_{[p\phi]}\dots$$
 there...  $D_{[g\phi]}$ 

· Blocking: some non-agreeing element intervenes on the tier

$$T_{[p\phi]} \dots C \dots D_{[g\phi]}$$

#### ■ Importance of the finite window ■

- Neither tiers nor the finite window alone are adequate.
  - Tiers allow long-distance dependencies to be treated as if local.
  - The finite constraint window limits the power of the system.
  - Together, they create the right type of relativized locality.

See Appendix A.3 and Appendix A.4 for details.

# 5 Typological variation

#### Parameters for variation

The parameters for TSL-2 (tier elements and constraints) correspond neatly to variation in long-distance dependencies.

- Visibility which elements are relevant and which are ignored?
  - Case-sensitive agreement (cf. Bobaljik 2008; Preminger 2014)
- Iteration if you allow AB and BB, then you get ABB, ABBB, etc.
  Case/gender/number concord
- Directionality do we ban AB or BA?
  - Upward/downward agreement (cf. Chomsky 2000; Zeijlstra 2012)

#### ■ Case-sensitive agreement ■

In Hindi, the verb agrees with the closest *nominative* argument, which may not be the subject.

- (1) Hindi verbal agreement ignores ergatives (Mahajan 1990)
  - a. Raam roTii khaataa thaa. Raam.**M.NOM** bread.**F**.NOM eat.IPFV.**M** be.PST.**M** 'Raam ate bread (habitually).'
  - b. Raam-ne roTii khaayii. Raam.**M-ERG** bread.**F**.NOM eat.PFV.**F** 'Raam ate bread.'

Analysis: Project D only if nominative. Tier constraints are unchanged.

#### ■ Case-sensitive agreement (2) ■

'Raam ate bread (habitually).' (Nominative subject, subject agrees)



We ignore agreement on the non-finite verb for simplicity. Concord will be discussed later.

#### ■ Case-sensitive agreement (3) ■

'Raam ate bread.' (Ergative subject, object agrees)



### ■ Ergative ≠ Invisible ■

Ergatives are not invisible in Nepali (though datives are).

- (2) Agreement with ergative in Nepali (Coon and Parker 2019)
  - a. Maile yas pasal-mā patrikaā kin-ē. **1SG.ERG** DEM store-LOC newspaper.ABS buy-**1SG** 'I bought the newspaper in this store.'
  - b. Ma thag-ī-ē.
    1sg.ABS cheat-PASS-1sg
    'I was cheated.'

No problem! We project  $D_{[NOM]}$  and  $D_{[ERG]}$  but not  $D_{[DAT]}$ .

# ■ Formal vs substantive constraints ■

- Case visibility hierarchy (Bobaljik 2008): Nom > Acc/Erg > Obliques
- We can encode the attested patterns in a TSL-2 grammar, but the implicational hierarchy itself requires a separate explanation.

# ■ Concord in the DP ■

To allow for iterated agreement, just permit  $p\phi \cdot p\phi$ .

(3) Gender concord in German
Ich habe [eine hübsche Muschel] gefunden.
I have [a.F pretty.F seashell.F] found
'I found a pretty seashell.'

1

**Analysis:** Ignore Mod on the tier, permit  $D_{[p\phi]} \cdot A_{[p\phi]}$  and  $A_{[p\phi]} \cdot A_{[p\phi]}$ .

# ■ Concord in the DP (2) ■

**Analysis:** Ignore Mod on the tier, permit  $D_{[p\phi]} \cdot A_{[p\phi]}$  and  $A_{[p\phi]} \cdot A_{[p\phi]}$ .



The Mod head is not crucial. If direct adjunction is used, then the pattern is local: the tier contains everything.

### Upward agreement

If the constraints are mirrored, then the direction of agreement is reversed.

(4) Case concord in German
 Ich habe [eine hübsche Muschel] gefunden.
 I have [a.ACC pretty.ACC seashell.ACC] found

Analysis: allow  $D_{[gCase]} \cdot A_{[pCase]}$  instead of  $D_{[pCase]} \cdot A_{[gCase]}$ , etc.

# ■ Upward agreement (2) ■

Analysis: allow  $D_{[gCase]} \cdot A_{[pCase]}$  instead of  $D_{[pCase]} \cdot A_{[gCase]}$ , etc.



We can handle definiteness agreement on the adjective (ignored here) in the same way.

# What does it mean to probe upward?

- In the MG derivation tree formalism (Graf and Shafiei 2019), we have a static representation of the entire derivation, so there is no problem.
- In a bottom-up Minimalist derivation, it is not obvious what it means for a probe to search upward. Some possibilities:
  - Let valued features search downward for unvalued features (Adger 2003)
  - Replace the search metaphor with the sliding window metaphor

#### Typological variation – summary

Example	Tier Elements	Tier Constraints	
(Canonical) subject-verb agreement	All T/D/C	Strict pairing of $p\phi$ and $g\phi$	
Case-sensitive agreement	All T/C D only if right case	(as above)	
Concord within DP	All D/Adj/N	Allow sequential $p\phi$	
Upward agreement	(as above)	Swap order of $p\phi/g\phi$	

# Parallels with phonology

Parameter	<i>φ</i> -agreement	Vowel harmony
Participants	Probe and most DPs	Most vowels
Invisible	Non-DPs, some DPs	Consonants, some vowels
Blockers	Finite C, some DPs	Some vowels
Directionality	Downward/upward	Progressive/regressive
Chaining	Concord/no concord	Spreading/"icy targets"

See McMullin (2016) and McMullin and Hansson (2016) regarding long-distance harmony.

# ■ What else is TSL? ■

Phenomenon	One line summary
Defective intervention*	Some DPs project even if they are never $g\phi$
Probe horizons (Keine 2019)	V/v/T/C project even if they are never $p\phi$
A'-agreement (Van Urk 2015)*	Only project DPs with a certain A' feature
Omnivorous number	Only project DPs with [PL], not [SG]
Upward C agr. (Diercks 2013)*	C probes up, only project DPs that EPP-move
Default agreement*	Allow lone $p\phi$ under limited circumstances
Interaction/Satisfaction (Deal 2015)*	Allow multiple $g\phi$ under limited circumstances
Independent subfeatures of $\phi$	Each probe gets its own tier/constraints

Also: many movement (Graf 2022b) and case patterns (Vu et al. 2019; Hanson 2023b), though these analyses use a different tier-based model.

\*See Hanson (2023a) and Hanson (2024a) for details.

#### ■ What isn't TSL? ■

Not all linguistic patterns are TSL. Of those that are not, most appear to be SS-TSL (structure-sensitive TSL). These include:

• Some long-distance harmony (De Santo and Graf 2019; Graf and Mayer 2018)

- Some tone patterns (e.g. unbounded tone plateauing)
- Some binding rules (Graf and Shafiei 2019)

# 6 Strengths and limitations of the model

#### Advantages of the model

- Clear separation of concerns:
  - Structural representation
  - Computations over said structure
  - Substance of elements of structure
- Insights:
  - Agreement is especially similar to harmony as both involve feature matching; the same seems to be true of movement
  - If case is different, this is plausibly because it involves different kinds of constraints (e.g. dependent case)

# Limitations of the model

Puzzles for the path-based approach:

- What to do about violations of c-command (e.g. sub-command)?
- How to handle exceptions to the complement spine generalization?

What the TSL model (alone) does not tell us:

- Why does case matter for *φ*-agreement? Why should nominatives always be visible, ergatives sometimes visible, and datives usually invisible?
- Why do probes seem to look downward more often than upward?
- How do children identify the visible elements and constraints for each dependency? (see Hanson 2024b; Belth 2023)

# 7 Conclusion

# ■ Summary ■

- Agreement patterns in syntax are largely TSL with a window size of 2.
- If we vary the tier projection and constraints slightly, we can account for a wide range of variation across languages and constructions.
- This variation is similar to other linguistic phenomena, especially phonological harmony.
- Most of the logical possibilities of the model are realized within a single phenomenon this is not necessarily expected!

# Some open questions

• Do we ever need a window size larger than 2?

- Are there patterns that are not TSL under any reasonable analysis?
- How far can we take the parallel with harmony in phonology?

#### Takeaways

- Computational approaches to linguistic analysis reveal insights that might otherwise not be obvious.
- In other cases, they provide independent support to conclusions reached in other ways (e.g. visibility is parameterized).
- A clear understanding of the formal patterns can help us understand other aspects of linguistic structure.

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# A Extras

A.1 Even more on TSL

#### Extra example: Sibilant harmony

Sibilants match in anteriority, t blocks harmony, other C's transparent

(based on Slovenian)

		]	sasasa	SSS	1
All elements:	{s, ∫, t, k, a}		s a <mark>s</mark> a∫a	s <mark>s</mark> ∫	X
Tier elements:	{s, ∫, t}		s a k a s a	S S	1
Constraints:	{*s∫, *∫s}		<mark>s</mark> aka∫a	<b>S</b> ∫	X
		1	satasa	s t s	1
			sata∫a	stſ	1

Word

Tier

#### TSL string languages – formal definition

In a **tier-based strictly** k-local (TSL-k) language, a string is well-formed iff its **tier projection** does not contain any forbidden substrings of some length k.

- $\Sigma$  = "alphabet" = set of all symbols
- T = "tier alphabet" = set of visible symbols
- G = "grammar" = forbidden substrings
- The tier projection is obtained by deleting all non-tier elements and concatenating the remaining elements.

#### **Example: vowel harmony (redux)**

		String	Tier projection	Substrings	
	$\Sigma = \{k, b, l, i, e, u, o, a\}$	kubulo	uuo	{uu,uo}	1
	$T = \{i, u, o, a\}$	kibilo	iio	{ii, <mark>io</mark> }	X
	$l_{r} = 2$	kubelo	uo	{uo}	1
	$\mathbf{K} = 2$	kibelo	io	{ <b>io</b> }	X
$G = \{iu, *ui, *io, *oi\}$	kubalo	uao	{ua,ao}	1	
		kibalo	iao	{ia,ao}	1

# A.2 Some formal details

# ■ MG derivation trees ■

- All nodes appear in base position.
- The rightmost child of a node is its complement; others are specifiers.
- Movement is indicated using feature diacritics.



See Graf and Kostyszyn (2021) for a formal definition. Related: Brody (2000).

#### ■ Command strings ■

- A command string (c-string) is a derivational ordering of nodes.
- There is a c-string from the root to each node.
- Among each head and its arguments: Head < Specifier < Complement.



See Graf and Shafiei (2019) for details.

### Tiers over command strings

 $\checkmark$  The cat **chases** the rats. (subject agreement)



# ■ Tiers over command strings (2) ■

**X** The cat **chase** the rats. (object agreement)



- A.3 More on locality
- Three models of locality

Immediate precedence (SL)



General precedence (SP)



# ■ Three models of locality (2) ■

- The immediate precedence (SL) model can handle local spreading.
- The general precedence (SP) model can handle unbounded processes, but can't handle blockers.
- Only the tier precedence (TSL) model can handle unbounded processes with blocking.

# A.4 Computational considerations

### ■ Limits on structural configurations ■

TSL computations can relate elements at a distance, but are otherwise severely restricted in what they can do.

- No arbitrary logic "a DP can A-move out of a finite CP, but only if there is A'-movement within some (other) CP in the sentence"
- No counting "up to three reflexive pronouns may occur in a sentence if each obeys the Binding Theory"

These characteristics derive from the restriction that all constraints must be stated within the moving window.

# ■ Conditions for efficient learning ■

- The restrictions on TSL patterns help to make them efficiently learnable by limiting the amount of memory needed (Lambert et al. 2021).
- But there are too many possible tiers to test them all individually.
- We also need to consider other aspects of language acquisition such as the Tolerance Principle (see eg. Belth 2023; Hanson 2024b).